

AMENDMENTS TO THE CLAIMS:

This listing of claims will replace all prior versions, and listings, of claims in the application:

LISTING OF CLAIMS:

1. (Currently Amended) A method of securely implementing a public-key cryptography algorithm in a microprocessor-based system, the public key being composed of an integer n that is a product of two large prime numbers p and q , and of a public exponent e , said algorithm also including a private key, said method ~~consisting in~~ determining a set E comprising a predetermined number of prime numbers e_i that can correspond to the value of the public exponent e , ~~said method being characterized in that it comprises and comprising~~ the following steps ~~consisting in~~:

a) computing a value $\epsilon = \prod_{e_i \in E} e_i$

such that ϵ/e_i is less than $\Phi(n)$ for any e_i belonging to E , where Φ is the Euler totient function;

b) applying the value ϵ to a predetermined computation involving, as a modular product, only the modular product of ϵ multiplied by said private key of the algorithm;

c) for each e_i , testing whether the result of said predetermined computation is equal to a value ϵ/e_i :

- if so, then attributing the value e_i to e , and storing e ~~with a view to it being used for subsequent use~~ in computations of said cryptography algorithm;

- otherwise, ~~observing~~ indicating that the computations of the cryptography algorithm using the value e cannot be performed.

2. (Currently Amended) A method according to claim 1, ~~characterized in that~~ wherein the cryptography algorithm is based on an RSA-type algorithm in standard mode.

3. (Currently Amended) A method according to claim 2, ~~characterized in that~~ wherein the predetermined computation of step b) ~~consists in~~ comprises computing a value C :

$C = \epsilon \cdot d$ modulo $\Phi(n)$, where d is the corresponding private key of the RSA algorithm such that $e \cdot d = 1$ modulo $\Phi(n)$ and Φ is the Euler totient function.

4. (Currently Amended) A method according to claim 2, ~~characterized in that~~ wherein the predetermined computation of step b) ~~consists in~~ comprises computing a value C :

$C = e \cdot d \text{ modulo } \phi(n)$, where d is the corresponding private key of the RSA algorithm such that $e \cdot d = 1 \text{ modulo } \phi(n)$, with ϕ being the Carmichael function.

5. (Currently Amended) A method according to claim 1, ~~characterized in that~~ wherein the cryptography algorithm is based on an RSA-type algorithm in CRT mode.

6. (Currently Amended) A method according to claim 5, ~~characterized in that~~ wherein the predetermined computation of step b) ~~consists in~~ comprises computing a value C :

$C = e \cdot d_p \text{ modulo } (p-1)$, where d_p is the corresponding private key of the RSA algorithm such that $e \cdot d_p = 1 \text{ modulo } (p-1)$.

7. (Currently Amended) A method according to claim 5, ~~characterized in that~~ wherein the predetermined computation of step b) ~~consists in~~ comprises computing a value C :

$C = e \cdot d_q \text{ modulo } (q-1)$, where d_q is the corresponding private key of the RSA algorithm such that $e \cdot d_q = 1 \text{ modulo } (q-1)$.

8. (Currently Amended) A method according to claim 5, ~~characterized in that~~ wherein the predetermined computation of step b) ~~consists in~~ comprises computing two values C_1 and C_2 such that:

$C_1 = e \cdot d_p \text{ modulo } (p-1)$, where d_p is the corresponding private key of the RSA algorithm such that $e \cdot d_p = 1 \text{ modulo } (p-1)$;

$C_2 = e \cdot d_q \text{ modulo } (q-1)$, where d_q is the corresponding private key of the RSA algorithm such that $e \cdot d_q = 1 \text{ modulo } (q-1)$;

and ~~in that~~ wherein the test step c) ~~consists~~ comprises, for each e_i , in testing whether C_1 and/or C_2 is equal to the value e/e_i :

- if so, then attributing the value e_i to e and storing e ~~with a view to it being used for~~ subsequent use in computations of said cryptography algorithm;

- otherwise, ~~observing~~ indicating that the computations of said cryptography algorithm using the value e cannot be performed.

9. (Currently Amended) A method according to claim 3 ~~or claim 4~~ and in which a value e_i has been attributed to e , ~~said method being characterized in that~~ wherein the computations using the value e ~~consist in~~ comprise:

choosing a random integer r ;

computing a value d^* such that $d^* = d + r \cdot (e \cdot d - 1)$; and

implementing a private operation of the algorithm in which a value x is obtained from a value y by applying the relationship $x = y^{d^*}$ modulo n .

10. (Currently Amended) A method according to ~~any one of claims 2 to 4, and claim 2,~~ in which a value e_i has been attributed to e , ~~said method being characterized in that it consists and further including the step,~~ after a private operation of the algorithm, ~~in of~~ obtaining a value x from a value y , and ~~in that wherein~~ the computations using the value e ~~consist in~~ comprise checking whether $x^e = y$ modulo n .

11. (Currently Amended) A method according to ~~any one of claims 5 to 8, and claim 5,~~ in which a value e_i has been attributed to e , ~~characterized in that it consists and further including the step,~~ after a private operation of the algorithm, ~~in of~~ obtaining a value x from a value y , and ~~in that wherein~~ the computations using the value e ~~consist in~~ comprise checking firstly whether $x^e = y$ modulo p and ~~secondly~~ whether $x^e = y$ modulo q .

12. (Currently Amended) A method according to ~~any preceding claim,~~ characterized ~~in that claim 1, wherein~~ the set E comprises at least the following e_i values: 3, 17, $2^{16}+1$.

13. (Currently Amended) An electronic component ~~characterized in that it comprises~~ comprising means for implementing the method according to ~~any preceding claim 1.~~

14. (Currently Amended) A smart card including ~~an~~ the electronic component ~~according to of~~ claim 13.

15. (Currently Amended) A method of securely implementing a public-key cryptography algorithm in a microprocessor-based system, the public key being composed of an integer n that is a product of two large prime numbers p and q , and of a public exponent e , said method ~~consisting in~~ determining a set E comprising a predetermined number of prime numbers e_i that can correspond to the value of the public exponent e , ~~said method being characterized in that it comprises and comprising~~ the following steps ~~consisting in:~~

- a) choosing a value e_i from the values of the set E ;
- b) if $\delta(p) = \delta(q)$, where $\delta(n)$, $\delta(p)$, and $\delta(q)$ are functions giving the number of bits encoding respectively the number n , the number p , and the number q , testing whether the chosen e_i value satisfies the relationship:

$$(1-e_i.d)\text{modulo } n < e_i.2^{(\delta(n)/2)+1}$$

or said relationship as simplified:

$$(-e_i.d)\text{modulo } n < e_i.2^{(\delta(n)/2)+1}$$

~~where $\delta(p)$, $\delta(q)$, and $\delta(n)$ are the functions giving the numbers of bits respectively encoding the number p, the number q, and the number n;~~

c) if the test relationship applied in the preceding step is satisfied ~~and so~~ defining $e = e_i$, and storing e with a view to using it for subsequent use in computations of said cryptography algorithm;

- otherwise, reiterating the preceding steps while choosing another value for e_i from the set E until an e_i value can be attributed to e and, if no e_i value can be attributed to e, then ~~observing~~ indicating that the computations of said cryptography algorithm using the value of e cannot be performed.

16. (Currently Amended) A method of securely implementing a public-key cryptography algorithm according to claim 15, ~~characterized in that it consists in performing wherein~~ step b is performed in the following manner when $\delta(p)[[#]] \neq \delta(q)$, i.e. when p and q are unbalanced, testing whether the chosen e_i value satisfies the following relationship:

$$(1-e_i.d) \text{ modulo } n < e_i.2^{g+1}$$

or said relationship as simplified:

$$(-e_i.d) \text{ modulo } n < e_i.2^{g+1}$$

with $g = \max(\delta(p), \delta(q))$, if $\delta(p)$ and $\delta(q)$ are known, or, otherwise, with $g = \delta(n)/2 + t$, where t designates the imbalance factor or a limit on that factor.

17. (Currently Amended) A method according to ~~claim 15 or claim 16, characterized in that~~ wherein, for all values of i, $e_i \leq 2^{16} + 1$, ~~and in that the step b) is replaced by another test step consisting in comprising:~~

b) if $\delta(p) = \delta(q)$, testing whether the chosen e_i value satisfies the relationship:

$$(1-e_i.d)\text{modulo } n < e_i.2^{(\delta(n)/2)+17}$$

or said relationship as simplified:

$$(-e_i.d)\text{modulo } n < e_i.2^{(\delta(n)/2)+17}$$

where $\delta(p)$, $\delta(q)$, and $\delta(n)$ are ~~the~~ functions giving the numbers of bits respectively encoding the number p, the number q, and the number n;

otherwise, when p and q are unbalanced, testing whether the chosen e_i value satisfies the following relationship:

$$(1-e_i.d) \text{ modulo } n < e_i.2^{g+17}$$

or said relationship as simplified:

$$(-e_i.d) \text{ modulo } n < e_i.2^{g+17}$$

with $g = \max(\delta(p), \delta(q))$, if $\delta(p)$ and $\delta(q)$ are known, or, otherwise, with $g = \delta(n)/2 + t$,

where t designates the imbalance factor or a limit on that factor.

18. (Currently Amended) A method according to ~~claim 15 or claim 16, characterized in that~~ wherein step b) is replaced with another test step ~~consisting in~~ comprising:

testing whether the chosen e_i value satisfies the relationship whereby:

a predetermined number of the first most significant bits of $(1-e_i.d)$ modulo n are zero;

or said relationship as simplified whereby:

said predetermined number of the first most significant bits of $(-e_i.d)$ modulo n are zero.

19. (Currently Amended) A method according to claim 18, ~~characterized in that~~ wherein the test is performed on the first 128 most significant bits.

20. (Currently Amended) A method according to ~~any one of claims 15 to 19, characterized in that~~ claim 15, wherein the cryptography algorithm is based on an RSA-type algorithm in standard mode.

21. (Currently Amended) A method according to ~~any one of claims 15 to 20, and in which~~ claim 15 wherein, when an e_i value has been attributed to e , ~~said method being characterized in that~~ the computations using the value e ~~consist in~~ comprise:

- choosing a random integer r ;
- computing a value d^* such that $d^* = d + r.(e.d - 1)$;

implementing a private operation of the algorithm in which a value x is obtained from a value y by applying the relationship $x = y^{d^*}$ modulo n .

22. (Currently Amended) A method according to ~~any one of claims 15 to 20 and in which~~ claim 15 wherein, when an e_i value has been attributed to e , ~~said method being characterized in that it consists,~~ after a private operation of the algorithm, ~~in obtaining a value x is obtained~~ from a value y and ~~in that~~ the computations using the value e ~~consist in~~ comprise checking whether $x_e = y$ modulo n .

23. (Currently Amended) A method according to ~~any one of claims 15 to 22,~~
~~characterized in that~~ claim 15, wherein the set E comprises at least the following e_i values: 3,
 17, $2^{16}+1$.

24. (Currently Amended) A method according to claim 23, ~~characterized in that~~
~~wherein~~ the preferred choice of the values e_i from the values of the set E is made in the
 following order: $2^{16}+1$, 3, 17.

25. (Currently Amended) An electronic component ~~characterized in that it comprises~~
~~comprising~~ means for implementing the method according to ~~any one of claims 15 to 24~~
claim 15.

26. (Currently Amended) A smart card including ~~an~~ the electronic component
~~according to~~ of claim 25 .

27. (New) A method according to claim 15, wherein, for all values of i , $e_i \leq 2^{16}+1$, step
 b) is replaced by another test step comprising:

b) if $\delta(p)=\delta(q)$, testing whether the chosen e_i value satisfies the relationship:

$$(1-e_i.d) \text{ modulo } n < e_i.2^{(\delta(n)/2)+17}$$

or said relationship as simplified:

$$(-e_i.d) \text{ modulo } n < e_i.2^{(\delta(n)/2)+17}$$

where $\delta(p)$, $\delta(q)$, and $\delta(n)$ are functions giving the numbers of bits respectively
 encoding the number p, the number q, and the number n;

otherwise, when p and q are unbalanced, testing whether the chosen e_i value
 satisfies the following relationship:

$$(1-e_i.d) \text{ modulo } n < e_i.2^{g+17}$$

or said relationship as simplified:

$$(-e_i.d) \text{ modulo } n < e_i.2^{g+17}$$

with $g=\max(\delta(p),\delta(q))$, if $\delta(p)$ and $\delta(q)$ are known, or, otherwise, with $g=\delta(n)/2+t$,
 where t designates the imbalance factor or a limit on that factor.

28. (New) A method according to claim 15, wherein step b) is replaced with another
 test step comprising:

testing whether the chosen e_i value satisfies the relationship whereby:

a predetermined number of the first most significant bits of $(1-e_i.d) \text{ modulo } n$ are zero;

or said relationship as simplified whereby:

said predetermined number of the first most significant bits of $(-e_i \cdot d)$ modulo n are zero.

29. (New) A method according to claim 4 and in which a value e_i has been attributed to e , wherein the computations using the value e comprise:

choosing a random integer r ;

computing a value d^* such that $d^* = d + r \cdot (e \cdot d - 1)$; and

implementing a private operation of the algorithm in which a value x is obtained from a value y by applying the relationship $x = y^{d^*}$ modulo n .